Abstract Authors

Kodaira and Spencer (1957) have studiedon the variation of almost complex structure. Hsiung (1966)has defined and studied structures and operators on almost Hermition manifolds. Also, Ogawa(1970) has studied operators on almost Hermition manifolds. In this paper, we have defined and studied structure and operators on almost Kaehlerian spaces and several theorems have been derived. We have also been demonstrated with in nearly Kaehlerian spaces that for the structure to be integrable, it is both necessary and sufficient that the square of the difference γ , i. e., $(\Gamma - \gamma)^2$ Γand between Additionally, when the operator Γ^2 vanishes across the entire space, then the space can be classified as Kaehlerian.

Keywords: Almost complex structure, almost Hermition spaces, almost Kaehlerian spaces, Kaehlerian spaces.

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I. INTRODUCTION

Consider Mⁿ as a Riemannian space, where its fundamental metric tensor is denoted as g_{ij} , and $g = det |g_{ij}|$. In this context, Greek indices i, j, k, and so on, range from 1 to n, which is the dimension of the space. Let $\varepsilon_{i_1,\ldots,i_p}^{j_1,\ldots,j_p}$ represent the generalized Kronecker's delta, and $\varepsilon_{i_1,\ldots,i_p}$ signify $\varepsilon_{i_1,\ldots,i_p}^{1,\ldots,p}$. We define F^p as the algebra of differential p-forms on M^n . Consequently, the operators of exterior differentiation $d: F^p \to F^{p+1}$, and the adjoint operator $d': \mathbf{F}^p \to \mathbf{F}^{n-p}$ can be expressed for a p-form $u = (u_{i_1, \dots, i_p})$ as follows:

$$(du)_{i_0,\dots,i_p} = \frac{1}{p!} \varepsilon_{i_0,\dots,i_p}^{\rho j_1,\dots,j_p} \nabla_{\rho} u_{j_1,\dots,j_p}$$
(1.1)

$$(d'u)_{i_1,\dots,i_{n-p}} = \frac{1}{p!} \sqrt{g} g^{\rho_1 j_1,\dots,g} g^{\rho_p j_p} u_{\rho_1,\dots,\rho_p} \varepsilon_{j_1,\dots,j_p i_1,\dots,i_{n-p}}$$
(1.2)

where ∇_j Represents the covariant differentiation concerning the Riemannian connection, the exterior co-differentiation $\delta:F^p o F^{p-1}$ is specified by

$$\delta = (-1)^{np+n+1} d' d d' \tag{1.3}$$

can be expressed locally as

$$(\delta u)_{i_2,\dots,i_p} \nabla^{\rho} u_{\rho i_2,\dots,i_p} \tag{1.4}$$

Let Δ be the Laplace-Beltrami operator defined by $\Delta = d\delta + \delta d$

Subsequently, utilizing equations (1.1) and (1.3), it is straightforward to confirm that in the case of a p – degree form u,

$$(\Delta u)_{i_1,\dots,i_p} = -\nabla^{\rho} \nabla_{\rho} u_{i_1,\dots,i_p} + + \sum_{i=1}^{p} R_{i_{\lambda}}^{\rho} u_{i_1,\dots,i_p}$$

$$(1.5)$$

$$+ \textstyle \sum_{\lambda < \mu} R_{i_\lambda i_\mu}{}^{\rho a} u_{i_1 \dots \widehat{\rho} \dots \widehat{a} \dots i_p}$$

holds, where R_{ijkl} (or R_{ij}) represents the curvature (or Ricci) tensor linked to the Riemann connection. In the notation $u_{i_1...\widehat{a}...i_p}$, the index ρ replaces the index i_{λ} , while in $u_{i_1...\widehat{a}....i_p}$ indicates that the subscript i_a is deleted.

If a Riemannian space M^n admits an almost complex structure A_i^j satisfying

$$g_{kh} A_i^k A_i^h = g_{ij} (1.6)$$

then it is called an almost Hermitian space. If in an almost Kaehler space, the Nijenhuis tensor satisfies the condition $N_{jih} + N_{jhi} = 0$, then we deduce from it $G_{jih} = 0$, i.e. $F_{i,i}^h + F_{i,i}^h = 0$ 0and the space is an almost Tachibana space. Thus, we have $3F_{ih,j} = F_{ji,h} = 0$. Consequently, the space is a Kaehler space i.e., an almost Kaehler space is a Kaehler space, if and only if the Nijenhuis tensor equation is satisfied.

Let $T^{c}(M)$ represent complexified tangent space of the manifold M^{n} . Consider F_{c}^{p} as the space of complexified differential p-forms, which are essentially complex-valued functions defined on $T^c(M) \wedge ... \wedge T^c(M)$. For non-negative integers r, s we introduce the projection mapping denoted by $\prod_{r,s} F_c^p \to F_c^p$ where p = r + s as follows:

$$\prod_{i}^{j} = \left(\frac{1}{2}\right) \left(\delta_{i}^{j} - \sqrt{-1}A_{i}^{j}\right) \tag{1.7}$$

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and its conjugate

$$\prod_{i}^{j} = \overline{\prod}_{i}^{j} = \left(\frac{1}{2}\right) \left(\delta_{i}^{j} + \sqrt{-1}A_{i}^{j}\right)$$
(1.8)

which will be abbreviated to \prod and $\overline{\prod}$ respectively. Then for a p-form \mathbf{u} of F_c^p , we define:

$$(\prod u)_{i_{2},\dots,i_{p}} = \left(\frac{1}{p!}\right) \prod_{i_{2},\dots,i_{p}}^{j_{1},\dots,j_{p}} u_{j_{1},\dots,j_{p}}$$

$$= \left[\frac{1}{(r!s!)}\right] \varepsilon_{i_{1},\dots,i_{r},i_{1},\dots,i_{r}}^{t_{1},\dots,t_{r},i_{1},\dots,i_{p}} \prod_{t_{1}}^{j_{1}} \dots \prod_{t_{r}}^{j_{r}} \prod_{h_{1}}^{k_{1}} \dots \prod_{t_{r}}^{k_{s}} u_{j_{1},\dots,j_{r},k_{1},\dots,k_{s}}.$$

$$(1.9)$$

A *p*-form u of F_c^p is called of type (r,s)if it satisfies ($\prod u$) = u.

Now, here following two Lemmas given by [Kodaira and Spencer (1957)], Ogawa (1970),

Lemma (1.1): In an almost complex space, for any set of functions u_{i_1,\ldots,i_p} , we have

$$\sum_{v=0}^{p} (\prod u)_{i_1,\dots,i_p} = u_{i_1,\dots,i_p}$$
 (1.10)

and

$$\sum_{v=0}^{p} {}_{p} C_{v} \varepsilon_{j_{1},...,j_{p}}^{\rho_{1},...,\rho_{p}} \prod_{\rho_{1}}^{j_{1}} \prod_{\rho_{v}}^{j_{v}} \overline{\prod_{\rho_{v+1}}^{j_{v+1}}} \overline{\prod_{\rho_{p}}^{j_{p}}} u_{j_{1},...,j_{p}}$$

$$= \varepsilon_{i_{1},...,i_{p}}^{j_{1},...,j_{p}} u_{j_{1},...,j_{p}}$$

$$(1.11)$$

holds for any $p\text{-form }u_{j_1,\dots,j_p}$, $1\leq p\leq n$.

Now we define the operators $d_1: F_c^p \to F_c^{p+1}$ of type (1,0) and $d_2: F_c^p \to F_c^{p+1}$ of type (2, -1) in accordance with [Kodaira and Spencer (1957)] given by

$$= \sum \prod d \prod, \tag{1.12}$$

r+s=p r+1,s r,s

$$d_2 = \sum_{r+s=p} \prod d_1 \quad d \quad \prod$$
 (1.13)

Here we denote the conjugate operator of d_1 (or d_2) by \bar{d}_1 (or \bar{d}_2).

Lemma (1.2): In an almost complex space, on
$$F_c^p$$
, we have
$$\prod_{r+3,s-2} d \prod = 0,$$
 (1.14)

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where, r + s = p.

From Lemmas (1.1) and (1.2), we have [2] [Kodaira and Spencer (1957)] given by
$$d = d_1 + d_2 + \bar{d}_1 + \bar{d}_2$$
 (1.15)

The definitions of complex counterparts of the real operators d and δ as per the framework established by Kodaira-Spencer in their (1957) work [2], can be stated as follows:

$$\partial = 2d_2 + d_1 - \bar{d}_2 \tag{1.16}$$

$$\mathfrak{D} = - * \partial * \tag{1.17}$$

On the other hand, Hsiung (1966) defined them by the following operators

$$(\partial u)_{i_0,\dots,i_p} = \left(\frac{1}{p!}\right) \sum_{i_0,\dots,i_p} \prod_{j_1,\dots,j_p}^{tj_1,\dots,j_p} \prod_{j_1}^{h} \nabla_h u_{j_1,\dots,j_p},$$
(1.18)

$$(\mathfrak{D}u)_{i_0,\dots,i_p} = -\sum_{t_{i_2},\dots,i_p} \prod_{t_i=1}^t \nabla^h u_{j_1,\dots,j_p},$$
(1.19)

for a p-form $u = (u_{i_1, \dots, i_n})$. After then we shall show that the relation

$$\mathfrak{D} = -* \boldsymbol{\partial} *$$
 is valid. (1.20)

II. OPERATORS ON ALMOST KAEHLERIAN MANIFOLDS

We have studied thefollowing properties of the operators

Lemma (2.1): In an almost Kaehlerian space, the operator Γ is askew-derivation and satisfies

$$*\Gamma * = -D \tag{2.1}$$

Proof: Ogawa (1967) gives that Γ is a skew-derivation and that for any p-form $u = u_{i_1, \dots, i_p}$, $(* \Gamma * u)_{i_2, \dots, i_p} = (-1)^{np+n+1} (Du)_{i_2, \dots, i_p}$ holds, where n is the dimension of the space. Since n is even, therefore (2.1) is proof.

Lemma (2.2): In an almost Kaehlerian space, the operator \emptyset is a derivation and satisfies for any *p*-form u_p ,

$$* \emptyset * u_p = (-1)^p \emptyset u_p \tag{2.2}$$

$$d\emptyset - \Box d = -\Gamma + Y \tag{2.3}$$

Proof: From directive calculation with respect to an orthonormal local coordinate system for any p-form $u = u_{i_1, \dots, i_n}$, we have

Since n is even, we have $(-1)^{p(n-p)} = (-1)^p$, and thus (2.2) is proved. Now, we have

$$\begin{array}{l} (d\emptyset u)_{i_0,...,i_p} = & \nabla_{i_0} A_{i_r}^t u & r & - & \nabla_{i_r} A_{i_0}^t u & r \\ & i_1,.....\widehat{t} \dots i_p & & i_1,....\widehat{t} \dots i_p \\ & - & \sum_{r \neq s} \nabla_{i_r} A_{i_s}^t & u & r & r & + A_{i_r}^t \nabla_{i_0} u & r \\ & & i_1,....\widehat{t} \dots i_p & & & & & \\ \end{array}$$

$$-A_{i_0}^t \nabla_{i_r} u \underset{i_1....\widehat{t}...i_p}{r} - \sum_{r \neq s} A_{i_s}^t \nabla_{i_r} u \underset{i_1...\widehat{t_0}...\widehat{t}...i_p}{r}$$

$$(\Box du)_{i_0,\ldots,i_p} = A_{i_0}^t \nabla_t u_{i_1,\ldots,i_p} - A_{i_s}^t \nabla_t u_{s_1,\ldots,i_0,\ldots,i_p}$$

$$\begin{array}{l} +A_{i_r}^t \nabla_{i_0} u {\begin{array}{*{20}{c}} r \\ i_1\widehat{t} \\i_p \end{array}} - \begin{array}{*{20}{c}} A_{i_0}^t \nabla_{i_r} u {\begin{array}{*{20}{c}} r \\ i_1\widehat{t} \\i_p \end{array}} \\ - \begin{array}{*{20}{c}} \sum_{r \neq s} A_{i_s}^t \nabla_{i_r} u {\begin{array}{*{20}{c}} s \\ i_0\widehat{t} \\\widehat{t} \\\widehat{t} \\i_p \end{array}}.$$

Hence it follows that

$$(d\emptyset u - \Box du)_{i_0,\dots,i_p} = (\nabla_{i_0} A^t_{i_r} - \nabla_{i_r} A^t_{i_0}) u \underset{i_1,\dots,\widehat{t},\dots,i_p}{r} - \sum_n (-1)^n A^t_{i_n} \nabla_t u_{i_0,\dots,\widehat{n},\dots,i_p}$$

$$+ \sum_{r < s} (-1)^r (\nabla_{i_r} A^t_{i_s} - \nabla_{i_s} A^t_{i_r}) u_{i_0 i_1 \dots \hat{r} \dots \hat{t} \dots \dots i_p}^{s}.$$

$$= \sum_{n < m} (-1)^{n} (\nabla_{i_{n}} A_{i_{m}}^{t} - \nabla_{i_{m}} A_{i_{n}}^{t}) u_{i_{0} \dots \hat{n} \dots \hat{t} \dots \dots i_{p}}^{m}$$

$$- \sum_{n} (-1)^{n} A_{i_{n}}^{t} \nabla_{t} u_{i_{0} \dots \dots \hat{n} \dots i_{p}}.$$

$$= (\Upsilon u - \Gamma u)_{i_0,\dots,i_p}.$$

Now, we have consider the following relation

Then, we have

Then, we have
$$(\Box u \wedge v)_{i_{1},\dots,i_{p+q}} + (u \wedge \Box v)_{i_{1},\dots,i_{p+q}} = \left(\frac{1}{(p!q!)}\right) \left[\sum_{r=1}^{p} \varepsilon_{i_{1},\dots,i_{p+q}}^{j_{1},\dots,j_{p+q}} A_{j_{r}}^{t} u \underset{j_{1},\dots,j_{p}}{\overset{s}{=}} v_{j_{p+1},\dots,j_{p+q}} \right. \\ + \sum_{s'=p+1}^{p+q} \varepsilon_{i_{1},\dots,i_{p+q}}^{j_{1},\dots,j_{p+q}} A_{j_{s'}}^{t} u_{j_{1},\dots,j_{p}} v \underset{j_{p+1},\dots,\widetilde{t},j_{p+q}}{\overset{s}{=}} \left. \left(\frac{1}{(p!q!)} \right) \sum_{n=1}^{p+q} A_{i_{n}}^{t} \varepsilon_{i_{1},\dots,i_{p+q}}^{j_{1},\dots,j_{p+q}} u_{j_{1},\dots,j_{p}} v_{j_{p+1},\dots,j_{p+q}} \right. \\ = \emptyset (u \wedge v)_{i_{1},\dots,i_{p+q}}$$

Thus, the operator \square is a derivation. From this, we have the following:

Corollary (2.1): In almost Kaehlerian space, the operator Y is a skew-derivation.

Corollary(2.2): In almost Kaehlerian space, the relation

$$d\Gamma + \Gamma d = d\Upsilon + \Upsilon d \tag{2.4}$$

holds.

Theorem(2.3): In almost Kaehlerian spacer, we have

$$*Y* = -\vartheta - i(\delta A) \tag{2.5}$$

where $i(\delta A)$ denotes the inner product with respect to a 1-form $\delta A(A=A_{ij})$

Proof: We have the definition of Y, forap-formu,

$$(Yu)_{i_0,\dots,i_p} = \sum_{n < m} (-1)^n T^t_{i_n i_m} u_{i_0,\dots,\hat{i},\dots,\hat{i}}^m m_{i_0,\dots,\hat{i},\dots,i_p},$$

Where, we write $T_{ij}^t = \nabla_i A_j^t - \nabla_j A_i^t$. Therefore we have

$$= [i(\delta A)u - \boldsymbol{\vartheta}u]_{i_2,\dots,i_p}.$$

Similarly, we have proof of the following:

Theorem (2.4): In an almost Kaehlerian space, we have

$$\boldsymbol{\partial} = (d - \sqrt{-1}\Gamma)/2\,,\tag{2.6}$$

$$\mathfrak{D} = (\delta - \sqrt{-1}D)/2, \tag{2.7}$$

$$\overline{\boldsymbol{\partial}} = (d + \sqrt{-1}\Gamma)/2, \qquad (2.8)$$

$$\bar{\mathfrak{D}} = (\delta + \sqrt{-1}D)/2, \qquad (2.9)$$

$$\boldsymbol{\partial} = \left[d - \sqrt{-1} \left(\Gamma - Y \right) \right] / 2, \qquad (2.10)$$

$$\mathfrak{D} = \left[\delta - \sqrt{-1} \{D - \vartheta - i(\delta A)\}\right] / 2, \qquad (2.11)$$

III. STRUCTURE ON ALMOST KAEHLERIAN SPACES

Theorem (3.1): In an almost Kählerian space, the structure's integrability is both a necessary and sufficient condition when:

$$(\Gamma - \Upsilon)^2 = 0.$$

Proof. We have the intergability condition of the almost complex structure is defined by $\partial^2 = 0$, given by [2] Kodaira and spencer(1957), Then by equation (2.10) $\partial^2 = \frac{1}{4} \left[-(\Gamma - Y)^2 + \sqrt{(-1)} \left(d\Gamma + \Gamma d - dY - Y d \right) \right]$,

$$\partial^2 = \frac{1}{4} \left[-(\Gamma - Y)^2 + \sqrt{(-1)} \left(d\Gamma + \Gamma d - dY - Y d \right) \right]$$

Considering that the imaginary components disappear due to the implication of Corollary (2.2), we derive the result: $\partial^2 = -\frac{1}{4} (\Gamma - Y)^2$ Which is real operator.

The operator Γwhich delineates a Kählerian structure through an almost Hermitian structure, demonstrates Kählerian characteristics only when the operator Γ^2 ceases to have an effect. As Γ functions as a skew-derivation, its second operation, Γ^2 , acts as a derivation.

Consequently, when Γ^2 nullifies its impact on forms of degrees 0 and 1, its influence dissipates across forms of all degrees. Taking into consideration a0-form f and a 1-form $u = (u_i)$, the following relationship holds:

$$(\Gamma^{2}f)_{ij} = (A_{i}^{t}\nabla_{t}A_{j}^{h} - A_{j}^{t}\nabla_{t}A_{i}^{h})\nabla_{h}f,$$

$$(\Gamma^{2}u)_{ijk} = \bigcup_{i,j,k} (A_{i}^{t}\nabla_{t}A_{j}^{h} - A_{j}^{t}\nabla_{t}A_{i}^{h})\nabla_{h}u_{k} + \bigcup_{i,j,k} (A_{i}^{t}A_{j}^{h}R_{thk}^{l})u_{l},$$

Where U_{ijk} indicates that the terms are summed cyclically with respect to I,i, j, k. Consequently, the condition $\Gamma^2 = 0$ can be expressed equivalently through the following relationships:

$$\left(A_i^t \nabla_t A_i^h - A_i^t \nabla_t A_i^h\right) = 0, \tag{3.1}$$

$$\bigcup_{i,j,k} \left(A_i^t A_j^h R_{thk}^l \right) = 0. \tag{3.2}$$

Theorem (3.2): In an almost Kaehlerian space, the operator Γ^2 consistently equals zero.

Proof: Since the complex structure A_i^j is a covariant constant in an Kaehlerian space, we have from $(3.1)A_i^tR_{tjk}^{\omega} = A_j^tR_{tik}^{\omega}$, and therefore $A_i^tA_j^hR_{thk}^{\omega} = R_{ijk}^{\omega}$, which gives (3.2) holds.

Theorem (3.3): In an almost Kaehlerian space, when $\Gamma^2 = 0$, if signifies that the structure is almost semi-Kaehlerian.

Proof: We have, Transvecting (3.1) with A_l^i , then $\nabla_l A_j^h + A_l^i A_j^t \nabla_t A_i^h = 0$. Contracting **l** and **h** and noting $A^{ih} \nabla_t A_{ih} = 0$. prove the theorem.

Theorem (3.4): If $\Gamma^2 = 0$ in an almost Kaehlerian space, then we have

$$\bigcup_{i,j,k} \left(A_i^t R_{jkt}^{\omega} \right) = 0 \tag{3.3}$$

$$\frac{1}{2} A^{th} R^{j}_{thi} + A^{t}_{i} R^{j}_{t} = 0, (3.4)$$

$$A_i^t R_{tj} + A_i^t R_{ti} (3.5)$$

Proof: Here, from equation (3.2), we get

$$A_i^t A_j^h A_k^l R_{thl}^\omega = A_i^t R_{ktj}^\omega - A_j^t R_{kti}^\omega$$
 (3.6)
Taking the sum of terms of (3.6) cyclically with respect to the indices **i**, **j**, **k**, we have

$$\bigcup_{i,j,k} \left(A_i^t A_j^h A_k^l R_{thl}^{\omega} \right) = \bigcup_{i,j,k} \left(A_i^t R_{jkt}^{\omega} \right) = 0.$$

gives (3.3). Contraction of **i** and ω in (3.3) yields

$$A^{it}R_{itjk} + A_j^t R_{tk} - A_k^t R_{tj} = 0. (3.7)$$

And, from equation (3.6) we get $-A_k^t A_i^h A_i^l R_{thl}^{\omega} = A_i^t R_{ktj}^{\omega} - A_k^t R_{itj}^{\omega} - A_j^t R_{kit}^{\omega}$,

Which can reduced to (3.4) by contracting with g^{ij} . Also, from (3.7) and (3.4), then we get the relation (3.5).

Theorem (3.5): If
$$\Gamma^2 = 0$$
 in an almost Kaehlerian space, then we have $\nabla^i A^{jk} \nabla_i A_{i\omega} = 0.$ (3.8)

Proof: We have, Differentiating (3.1) by ∇_i , then

$$A^{it} \nabla_i \nabla_t A^h_j = \nabla^i A^t_j \nabla_t A^h_i + A^t_j (R^i_{itl} A^{lh} + R^h_{itl} A^{il}).$$
 From (3.4) and (3.5) and noting above equation, we get

Here, the second and third terms on the right- hand side are reduced to $-R_i^h$ and R_i^h , respectively and thus we have (3.8).

Theorem (3.6): If the operator Γ^2 vanishes everywhere in an almost Kaehlerian space, it implies that the space is Kaehlerian.

Proof: Here, firstly we prove that

$$A^{jk} \nabla^t \nabla_t A_{jk} = 0. (3.9)$$

Then, by virtue of (3.1) we find $\nabla_i A_i^h = A_i^h A_l^t \nabla_t A_i^l$

the above equation and (3.8) and (3.5) gives $\nabla^i \nabla_i A_i^h = A_i^h \nabla^i A_i^t \nabla_t A_i^l$

Now contracting above equation with A_h^j and noting theorem (3.5), we obtain (3.9). From equation (3.9) follows immediately $\nabla^i A^{jk} \nabla_i A_{jk} = \left(\frac{1}{2}\right) \nabla^i \nabla_i \left(A^{jk} A_{jk}\right) - A^{jk} \nabla^i \nabla_i A_{jk} =$ 0. Which means $\nabla_i A_{jk} = 0$. proving the structure to be Kaehlerian.

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