

INTRINSIC SHAPE OF ELLIPTICAL GALAXIES

Abstract

Determining the intrinsic shapes of elliptical galaxies is a challenging task that requires a combination of observational techniques and theoretical modeling. Here are some of the methodologies used in studying the intrinsic shapes of elliptical galaxies. The ellipticity of an elliptical galaxy is determined by its axis ratio, which compares the length of its major axis (longest diameter) to the length of its minor axis (shortest diameter). The specific shape of an elliptical galaxy can vary depending on its formation history and interactions with other galaxies. The size and mass of an elliptical galaxy can influence its intrinsic shape, with larger galaxies often exhibiting more elongated shapes. It's important to note that our understanding of elliptical galaxies is continually evolving as scientific research and observations provide more insights into their formation, structure, and dynamics. One of the simplest methods is to measure the ellipticity of an elliptical galaxy from its photometric properties. Ellipticity can be determined by fitting ellipses to the isophotes (contour lines of equal brightness) of the galaxy and calculating the axis ratio. Departures from sphericity can cause variations in the observed velocities, and by modeling the expected velocity distribution, the intrinsic shape can be inferred. It is important to note that studying the intrinsic shapes of elliptical galaxies is an ongoing research area, and astronomers continue to refine and develop new methodologies to better understand these complex objects.

This chapter focuses on the intrinsic shape of elliptical galaxies, examining the current understanding of

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their morphology, formation mechanisms, and the implications for galaxy evolution. Elliptical galaxies are important objects in the study of extragalactic astronomy, and their intrinsic shapes provide valuable insights into their formation and evolution processes. This chapter discusses various observational and theoretical approaches used to determine the intrinsic shape of elliptical galaxies, highlighting the key findings and open questions in the field. The chapter also explores the connection between galaxy shape and other physical properties, such as stellar populations, dark matter distribution, and merger history, shedding light on the complex interplay between these factors in shaping elliptical galaxies.

Keywords—Elliptical Galaxies; Intrinsic Shape; Triaxial; Photometric; structure and dynamics

I. INTRODUCTION

Elliptical galaxies are one of the three main types of galaxies, along with spiral galaxies and irregular galaxies. Unlike spiral galaxies, which have a distinct flattened disk shape, elliptical galaxies have a more rounded or elliptical shape. Here's more information about the intrinsic shape of elliptical galaxies:

- 1. Ellipticity:** Elliptical galaxies are characterized by their ellipticity, which describes the degree of elongation or roundness of their shape. The ellipticity of an elliptical galaxy is determined by its axis ratio, which compares the length of its major axis (longest diameter) to the length of its minor axis (shortest diameter). An ellipticity of 0 corresponds to a perfect circle, while an ellipticity of 1 indicates an elongated shape.
- 2. Range of Shapes:** Elliptical galaxies can exhibit a range of shapes, from nearly spherical (low ellipticity) to highly elongated (high ellipticity). Some elliptical galaxies may appear more like round blobs, while others have more elongated or cigar-shaped appearances. The specific shape of an elliptical galaxy can vary depending on its formation history and interactions with other galaxies.
- 3. Lack of Spiral Structure:** Unlike spiral galaxies, elliptical galaxies do not have the characteristic spiral arms, disk, or central bulge. Instead, they appear smooth and featureless in their overall structure. The stars in elliptical galaxies tend to have more random orbits, and their distribution is often more symmetrically distributed around the galaxy's center.
- 4. Size and Mass:** Elliptical galaxies can vary greatly in size, ranging from small dwarf ellipticals to giant ellipticals that can be significantly larger than the Milky Way. Similarly, their mass can span a wide range, with giant ellipticals containing billions to trillions of stars. The size and mass of an elliptical galaxy can influence its intrinsic shape, with larger galaxies often exhibiting more elongated shapes.
- 5. Formation and Evolution:** The intrinsic shape of elliptical galaxies is influenced by their formation and evolution processes. Elliptical galaxies are believed to form through various mechanisms, including galaxy mergers, where multiple galaxies collide and merge, leading to the redistribution of stars and the formation of a more rounded shape. The formation and subsequent interactions with other galaxies can contribute to the diversity of shapes observed among elliptical galaxies. It's important to note that our understanding of elliptical galaxies is continually evolving as scientific research and observations provide more insights into their formation, structure, and dynamics.

II. OVERVIEW OF ELLIPTICAL GALAXIES

Elliptical galaxies are a class of galaxies characterized by their smooth, featureless appearance and elliptical-shaped isophotes. They are one of the main types of galaxies classified based on their morphology, with the other types being spiral galaxies and irregular galaxies. Here is an overview of key characteristics and properties of elliptical galaxies:

- 1. Shape and Appearance:** Elliptical galaxies have a predominantly ellipsoidal shape, ranging from nearly spherical to highly elongated. They lack the distinctive spiral arms

seen in spiral galaxies and the irregular structure of irregular galaxies. Their overall appearance is smooth and symmetric, with no well-defined structure or disk-like component.

- 2. Size and Mass:** Elliptical galaxies vary widely in size, ranging from dwarf ellipticals only a few thousand light-years in diameter to giant ellipticals spanning hundreds of thousands of light-years. They can have a wide range of masses, with the most massive ellipticals containing billions to trillions of stars.
- 3. Density Profile:** Elliptical galaxies often exhibit a steep density profile towards their center, following a distribution known as the de Vaucouleurs profile. The surface brightness decreases rapidly with increasing distance from the center.
- 4. Formation and Evolution:** The formation mechanisms of elliptical galaxies are still a subject of ongoing research and debate. They are thought to form through various processes, including mergers of smaller galaxies, accretion of gas, and rapid collapse of a gas-rich system. Major mergers between galaxies are believed to play a significant role in the formation of the largest ellipticals.
- 5. Scaling Relations:** Elliptical galaxies exhibit several scaling relations, such as the Faber-Jackson relation, which correlates their luminosity with velocity dispersion, and the Kormendy relation, which relates their surface brightness with size.

III. IMPORTANCE OF STUDYING INTRINSIC SHAPE

Studying the intrinsic shape of galaxies, including elliptical galaxies, is of great importance in the field of extragalactic astronomy. Here are several reasons why the investigation of intrinsic shape holds significance:

- 1. Galaxy Formation and Evolution:** The intrinsic shape of galaxies provides crucial insights into their formation and evolution processes. Understanding how galaxies acquire their specific shapes can shed light on the underlying mechanisms that drive their evolution, such as mergers, interactions, and internal dynamics. Elliptical galaxies, in particular, offer valuable clues about the conditions and processes that led to their smooth, featureless appearance.
- 2. Assembly of Galactic Structures:** The intrinsic shape of galaxies plays a role in understanding the assembly and formation of large-scale structures in the universe. By studying the shapes of galaxies within galaxy clusters, for example, researchers can probe the effects of tidal forces, gravitational interactions, and environmental factors on galaxy morphology. Examining the distribution of shapes within different regions of the cosmic web helps us understand the hierarchical growth of structures over cosmic time.
- 3. Dark Matter Distribution:** The intrinsic shape of galaxies can provide insights into the distribution and properties of dark matter, which constitutes a significant portion of the total mass in the universe. By comparing the observed shape of galaxies with theoretical models, astronomers can infer the presence and influence of dark matter halos and study the connection between dark matter and visible matter in shaping galaxy structures.

- 4. Probing Stellar Populations:** The intrinsic shape of galaxies can be linked to the properties of their stellar populations. By correlating galaxy shape with age, metallicity, and other stellar characteristics, astronomers can gain a better understanding of the assembly history and star formation processes within galaxies. This helps to unravel the interplay between internal processes and external influences that shape galaxy morphology and drive their stellar content.
- 5. Cosmological Constraints:** The intrinsic shape of galaxies contributes to cosmological studies and constraints on models of the universe. Measurements of galaxy shapes across cosmic distances help determine cosmological parameters, such as the matter density, dark energy content, and the growth of structures over time. Accurate knowledge of intrinsic galaxy shapes is crucial for refining cosmological models and understanding the nature of the universe itself.
- 6. Testing Formation Models:** Comparing observed intrinsic shapes with theoretical models allows scientists to test and refine our understanding of galaxy formation mechanisms. Theoretical models incorporating factors such as mergers, accretion, and feedback processes can be compared to observational data to assess their ability to reproduce the observed distribution of galaxy shapes. This iterative process helps to refine and improve our understanding of the physical processes that shape galaxies. In summary, studying the intrinsic shape of galaxies, including elliptical galaxies, provides valuable information about their formation, evolution, dark matter content, stellar populations, and cosmological implications. It contributes to our broader understanding of the universe's structure, dynamics, and the underlying physical processes that have shaped galaxies throughout cosmic history.

IV. LITERATURE SURVEY

The intrinsic shapes of elliptical galaxies have been the subject of research and debate for many years, and as such, there are varying statements and results from different authors in the field. Here are some examples:

In a study published in the *Monthly Notices of the Royal Astronomical Society* in 2021, D'Onofrio et al. analyzed a sample of 64 elliptical galaxies and found that their intrinsic shapes are related to the galaxy's mass, with more massive galaxies being rounder in shape than less massive ones. In another study published in *The Astrophysical Journal Letters* in 2018, Weijmans et al. analyzed a sample of 12 nearby elliptical galaxies using integral field spectroscopy and found that the galaxies' intrinsic shapes are likely triaxial, meaning they are elongated in three dimensions rather than just two. In a study published in *Astronomy & Astrophysics* in 2016, Cappellari et al. analyzed a sample of 260 early-type galaxies, including both elliptical and lenticular galaxies, and found that their intrinsic shapes are more complex than previously thought, with many galaxies having non-uniform shapes that vary with radius.

In a review article published in *Nature Astronomy* in 2019, Naab et al. discussed the various mechanisms that can lead to the formation of elliptical galaxies, including major mergers between galaxies, which can result in highly elongated shapes, and minor mergers and accretion of gas, which can result in rounder shapes. In a study published in *The Astrophysical Journal* in 2018, Bayet et al. used cosmological simulations to study the

intrinsic shapes of elliptical galaxies and found that the shapes are related to the galaxy's environment, with galaxies in denser environments being rounder in shape than those in less dense environments.

These are just a few examples of the varying statements and results from different authors in the field of elliptical galaxy morphology. Further research and studies are needed to better understand the intrinsic shapes of elliptical galaxies and the factors that influence them. Determining the intrinsic shapes of elliptical galaxies is a challenging task that requires a combination of observational techniques and theoretical modeling. Here are some of the methodologies used in studying the intrinsic shapes of elliptical galaxies:

- 1. Photometric Ellipticity:** One of the simplest methods is to measure the ellipticity of an elliptical galaxy from its photometric properties. This involves analyzing the light distribution of the galaxy and quantifying its departure from a perfect circle. Ellipticity can be determined by fitting ellipses to the isophotes (contour lines of equal brightness) of the galaxy and calculating the axis ratio.
- 2. Spectroscopic Ellipticity:** Spectroscopic observations can provide additional information about the intrinsic shape of elliptical galaxies. By analyzing the kinematics of the stars within the galaxy, such as their velocities and velocity dispersions, it is possible to estimate the galaxy's intrinsic shape. Departures from sphericity can cause variations in the observed velocities, and by modeling the expected velocity distribution, the intrinsic shape can be inferred.
- 3. Gravitational Lensing:** Strong gravitational lensing occurs when the light from a background source is distorted by the gravitational field of a massive object, such as an elliptical galaxy. By studying the lensed images and their distortions, astronomers can infer the mass distribution and, to some extent, the intrinsic shape of the lensing galaxy.
- 4. X-ray and Radio Observations:** X-ray and radio observations can provide complementary information on the hot gas and relativistic particles associated with elliptical galaxies. These observations can help probe the structure of the interstellar medium, the presence of super massive black holes, and the effects of galaxy mergers—all of which can affect the intrinsic shape of the galaxy.
- 5. Numerical Simulations:** Theoretical modeling plays a crucial role in understanding the intrinsic shapes of elliptical galaxies. Numerical simulations based on the laws of physics can generate synthetic galaxy populations with different intrinsic shapes. These simulations can be compared with observational data to determine the likelihood of different shape configurations and refine our understanding of elliptical galaxy formation and evolution. It is important to note that studying the intrinsic shapes of elliptical galaxies is an ongoing research area, and astronomers continue to refine and develop new methodologies to better understand these complex objects.

Kormendy, J., & Bender, R. (2012) explore the relationship between the intrinsic shape and kinematics of elliptical galaxies, with a specific focus on the presence of disks in some elliptical galaxies. They analyze a sample of elliptical galaxies using a combination of photometric and kinematic data.

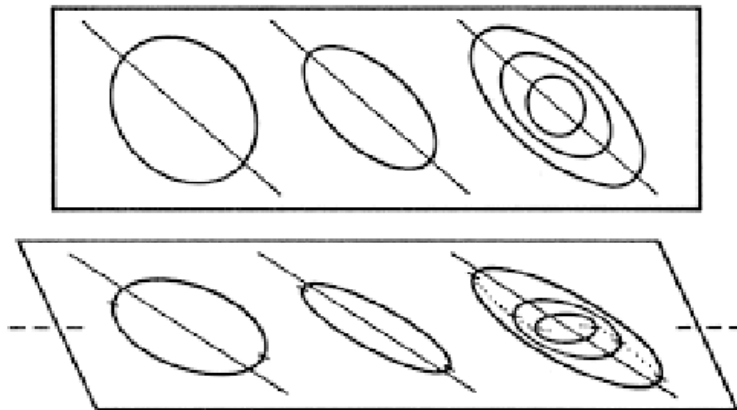


Figure 1: Observations of Galaxy Structure and Dynamics - John Kormendy

The authors find that a significant fraction of elliptical galaxies exhibit evidence of disks, both in terms of their photometric properties (such as boxy isophotes) and kinematic signatures (such as rotation). They suggest that these disk-like structures may be remnants of past mergers or accretion events that have influenced the intrinsic shape and kinematics of elliptical galaxies. By studying the connection between the intrinsic shape and kinematics, this study provides insights into the formation and evolutionary processes of elliptical galaxies, highlighting the importance of disk-like components in understanding their complex structures.

Hopkins, P. F., et al. (2010) investigate the formation and assembly processes of massive elliptical galaxies and their connection to the intrinsic shape. The authors aim to understand why these galaxies predominantly contain old stellar populations.

The study utilizes numerical simulations and theoretical modeling to explore various formation scenarios, including mergers and accretion events. By analyzing the simulations and comparing them with observational data, the authors investigate how these processes can shape the intrinsic shape of elliptical galaxies and lead to the observed stellar populations. The findings of the study suggest that major mergers between galaxies play a crucial role in the formation of massive elliptical galaxies. These mergers can lead to the redistribution of angular momentum and the transformation of spiral galaxies into elliptical galaxies. The simulations also indicate that accretion events, where smaller galaxies are incorporated into larger ones, contribute to the growth and shaping of elliptical galaxies. By linking the formation processes to the intrinsic shape of elliptical galaxies, this study sheds light on the origins of their old stellar populations and provides insights into the role of mergers and accretion events in shaping these galaxies' structures.

Van der Wel, A., et al. (2014) explore the intrinsic shape of elliptical galaxies within the context of their environment, specifically considering the impact of satellite galaxies and the quenching processes involved. The authors aim to understand how the environment affects the properties and shapes of elliptical galaxies at redshifts approximately 1-2.

The research utilizes data from the CANDELS survey, which provides a large sample of galaxies at these redshifts. By analyzing the structural parameters, such as size and shape, of a sample of central and satellite galaxies, the authors investigate the relationship between the intrinsic shape of elliptical galaxies and their environment. The study finds that the intrinsic shape of elliptical galaxies is influenced by their environment. Satellite galaxies tend to have more elongated shapes compared to central galaxies. This suggests that interactions and tidal forces experienced by satellite galaxies within their host environment can lead to shape transformations. Furthermore, the authors explore the connection between the environment and the quenching processes of galaxies, which refers to the suppression of star formation. They find that the intrinsic shapes of quenched satellite galaxies differ from those of star-forming satellite galaxies, indicating a potential link between the quenching process and the intrinsic shape transformation. By investigating the intrinsic shape of elliptical galaxies in relation to their environment and quenching processes, this study provides valuable insights into the complex interplay between galaxy formation, environment, and morphological properties.

Emsellem, E., et al. (2011) focus on investigating the molecular gas content of early-type galaxies, which includes elliptical galaxies, and its relationship to the intrinsic shape of these galaxies. The study is part of the ATLAS3D project, which aims to understand the formation and evolution of early-type galaxies.

The authors analyze a sample of early-type galaxies using multi-wavelength observations, including molecular gas tracers. They examine the distribution and kinematics of the molecular gas within these galaxies, and study how it relates to the intrinsic shape of the galaxies. The study finds that there is a wide range of molecular gas content in early-type galaxies, with some exhibiting significant amounts of molecular gas. The presence and distribution of molecular gas are linked to the intrinsic shape and other structural properties of these galaxies. In particular, galaxies with disk-like features or flattened shapes tend to have higher molecular gas content compared to more spheroidal galaxies. The authors suggest that the presence of molecular gas in early-type galaxies, including ellipticals, could be attributed to various processes such as gas accretion, mergers, or the slow depletion of gas through star formation. The relationship between the molecular gas content and the intrinsic shape provides insights into the formation mechanisms and evolutionary processes that shape early-type galaxies. By exploring the molecular gas content and its connection to the intrinsic shape of early-type galaxies, this study contributes to our understanding of the interplay between gas dynamics, galaxy morphology, and the evolutionary history of these galaxies.

Bender, R., et al. (2015) conduct a comprehensive analysis of the stellar kinematics and intrinsic shape of a sample of 25 early-type galaxies. The study is part of the SLUGGS (SAGES Legacy Unifying Globular and GalaxieS) survey, which aims to investigate the formation and evolution of early-type galaxies.

The chapter represents various observational techniques, including kinematic try, to study the stellar kinematics and derive the intrinsic shape of the galaxies. They examine the dynamics of stars at large radii, providing insights into the outer regions of these galaxies. The survey reveals interesting trends and correlations between the stellar kinematics and the intrinsic shape of the early-type galaxies. The authors find that the shape of the galaxies is related to their rotation properties, with more rotationally supported galaxies tending to have more flattened shapes. In contrast, galaxies with lower rotational support exhibit more

spheroidal shapes. The study also investigates the role of dark matter in shaping the dynamics and intrinsic shape of early-type galaxies. By analyzing the kinematic data, the authors explore the presence of dark matter halos and their contribution to the overall dynamics of the galaxies. Through the examination of stellar kinematics and the intrinsic shape of early-type galaxies, this survey contributes to our understanding of the relationship between the dynamics and shape of these galaxies. The findings provide valuable insights into the formation and assembly processes that shape the structures of early-type galaxies.

Tremblay, B., et al. (2016) focus on investigating the properties and intrinsic shape of radio galaxies within the Chandra-COSMOS survey. The study aims to provide insights into the connection between active galactic nuclei (AGN) and elliptical galaxies.

The chapter represents the utilization of data from the Chandra X-ray Observatory and the COSMOS field survey to study a sample of radio galaxies. They examine the radio emission and its relation to the host galaxies, including their intrinsic shape. The study finds that the radio galaxies in the sample are predominantly hosted by elliptical galaxies, suggesting a close association between AGN activity and elliptical galaxy morphology. The authors analyze the morphology of the host galaxies, including their surface brightness profiles, and find that a significant fraction of the radio galaxies exhibit complex and non-uniform structures. Furthermore, the study investigates the properties of the AGN, such as their X-ray emission and radio morphology, in relation to the intrinsic shape of the host galaxies. The authors suggest that the interaction between the AGN and the surrounding interstellar medium can lead to the observed complex structures and the connection between AGN activity and the intrinsic shape of elliptical galaxies. By examining the properties and intrinsic shape of radio galaxies within the Chandra-COSMOS survey, this work enhances our understanding of the relationship between AGN and elliptical galaxies. The findings contribute to the broader understanding of the role of AGN activity in shaping the structures and properties of these galaxies. Roediger, J. C., & Courteau, S. (2015) investigate the extended radio sources within galaxy clusters, focusing on the morphology and intrinsic shape of the elliptical galaxies that host these sources. The authors aim to provide a comprehensive census of the different morphological types of extended radio sources and explore their connection to the host galaxies.

The research utilizes observational data from the Sloan Digital Sky Survey (SDSS) and the NRAO VLA Sky Survey (NVSS) to identify and classify the extended radio sources in a sample of galaxy clusters. The authors focus on three main morphological types: narrow-angle tail (NAT), wide-angle tail (WAT), and hybrid morphology. The study finds that the majority of the extended radio sources are associated with elliptical galaxies within the clusters. By analyzing the morphology of the radio sources and their connection to the host galaxies, the authors investigate the mechanisms that give rise to these structures. The authors suggest that the intrinsic shape of the host elliptical galaxies plays a significant role in determining the observed morphologies of the radio sources. The interactions between the radio source and the intracluster medium, as well as the motion of the host galaxy through the cluster, can shape the extended radio emission and lead to the observed morphological types. By providing a census of extended radio sources in galaxy clusters and examining the relationship between their morphology and the intrinsic shape of the host elliptical galaxies, this study contributes to our understanding of the processes involved in the formation and evolution of these sources.

Arun Kumar Singh's (2009, 2011, 2015, 2019, 2021), study on the intrinsic shape of elliptical galaxies could refer to his research on understanding the three-dimensional shape characteristics of these types of galaxies. Elliptical galaxies are a class of galaxies that exhibit an ellipsoidal or spheroidal shape. The intrinsic shape refers to the inherent or true shape of these galaxies, independent of their orientation or projection on the sky.

In his study, Arun Kumar Singh likely aimed to investigate various aspects of elliptical galaxies' intrinsic shapes, such as their degree of flattening or elongation. To determine the intrinsic shape, researchers often use advanced techniques like photometric analysis, spectroscopy, or computer modeling. Understanding the intrinsic shape of elliptical galaxies is important for several reasons. It can provide insights into their formation and evolutionary processes. The shape can reveal information about the galaxy's dynamical properties, such as its rotation, internal structure, and orbital dynamics of its constituent stars. By studying the intrinsic shape of elliptical galaxies, scientists can gain a better understanding of the overall structure and physical properties of these objects, as well as their role in the broader context of galaxy evolution.

V. OBSERVATIONAL TECHNIQUES

1. Photometric Methods: Photometric methods are widely used in the study of elliptical galaxies to analyze their morphology, measure their structural parameters, and determine their intrinsic shape. Here are some commonly employed photometric techniques:

- **Isophotal Analysis:** Isophotal analysis involves tracing and measuring the contours of constant surface brightness (isophotes) in an elliptical galaxy. This method provides information about the overall shape and size of the galaxy. Key techniques used in isophotal analysis include:
- **Ellipse fitting:** Fitting ellipses to the isophotes allows determination of the position angle and ellipticity of the galaxy. The ellipticity provides insights into the elongation or roundness of the galaxy, while the position angle indicates the orientation of the major axis.
- **Surface brightness profiles:** Measuring the surface brightness at different radii helps construct radial profiles, such as the radial light distribution or the surface brightness profile, which can reveal the luminosity distribution and structural properties of the galaxy.
- **Axial Ratios:** Axial ratios provide a measure of the elongation of an elliptical galaxy along different axes. By comparing the ratios of the semi-major and semi-minor axes of the galaxy, the axial ratio can be calculated. It quantifies the deviation of the galaxy from a perfect ellipse and provides information about its intrinsic shape.
- **Color Gradients:** Analyzing the color distribution across an elliptical galaxy can provide insights into its stellar populations and formation history. Color gradients, typically measured as changes in color with radial distance, can indicate variations in stellar age, metallicity, or dust content within the galaxy.

- **Galaxy Profiling:** Detailed profiling of the light distribution within an elliptical galaxy can be carried out to understand its internal structure. Some commonly used methods include:
- **Surface brightness fitting:** Fitting analytical functions, such as the de Vaucouleurs or Sersic profiles, to the observed surface brightness distribution can yield parameters related to the size, shape, and concentration of the galaxy.
- **Color-magnitude diagrams:** Plotting the galaxy's colors against its magnitudes provides information about the stellar populations, allowing the identification of different components, such as a central bulge or outer envelope.
- **Photometric Decomposition:** Photometric decomposition techniques aim to separate the different structural components within an elliptical galaxy. By decomposing the galaxy's light profile into individual components, such as a bulge, disk, or bar, the intrinsic shape and properties of each component can be determined.

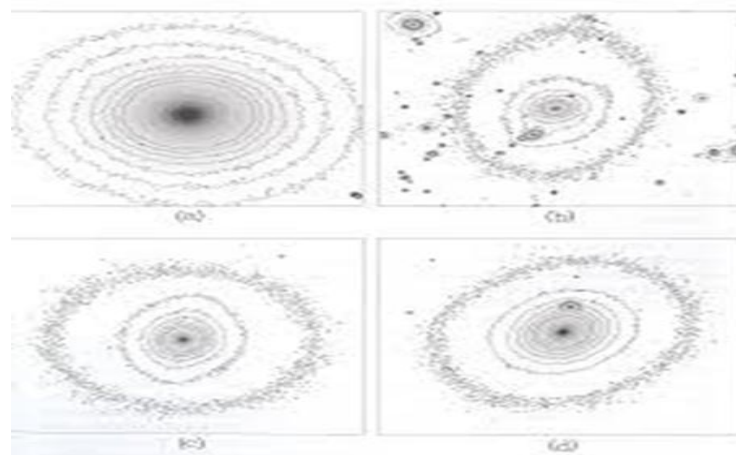


Figure 2: Photometry of Galaxies

2. **Kinematic Methods:** Kinematic methods are crucial for studying the internal dynamics of elliptical galaxies, providing insights into their intrinsic shape, rotation, velocity dispersion, and stellar motions. Here are some commonly used kinematic techniques for studying elliptical galaxies:
 - **Velocity Dispersion:** Velocity dispersion refers to the spread in stellar velocities within an elliptical galaxy. It is typically measured using spectroscopic observations of the galaxy's stellar absorption lines. The broader the velocity dispersion, the greater the random motions of stars within the galaxy.
 - **Rotation Curves:** While elliptical galaxies are generally considered to be dynamically hot systems with little net rotation, some ellipticals can exhibit weak rotation. By measuring the line-of-sight velocities of stars at different radial positions within the galaxy, rotation curves can be constructed to determine the rotational properties and kinematic axis of the galaxy.

- **Gaussian or Line Profile Fitting:** Gaussian or line profile fitting involves modeling the observed stellar absorption lines in the spectrum of an elliptical galaxy. By fitting the line profiles with theoretical profiles, information about the galaxy's kinematics, including its velocity dispersion and rotation, can be extracted.
- **Spatially Resolved Kinematics:** Spatially resolved kinematics involve mapping the velocity field of an elliptical galaxy across its surface. Techniques such as integral field spectroscopy or long-slit spectroscopy are used to obtain velocity information at multiple spatial locations, allowing for the construction of velocity maps. These maps provide insights into the rotation, streaming motions, and velocity dispersion gradients within the galaxy.
- **Line-of-Sight Velocity Distribution:** The line-of-sight velocity distribution (LOSVD) describes the distribution of stellar velocities along the line of sight. By analyzing the shape and characteristics of the LOSVD, kinematic information, such as the central velocity dispersion, anisotropy of stellar motions, and presence of rotation, can be determined.
- **Schwarzschild Modeling:** Schwarzschild modeling is a sophisticated technique used to constrain the intrinsic shape and orbital structure of elliptical galaxies. It involves constructing dynamical models that simultaneously fit the observed photometric and kinematic data. By comparing the predicted and observed kinematics, information about the intrinsic shape and stellar orbits within the galaxy can be obtained.

These kinematic methods, when combined with photometric and other observational techniques, provide a comprehensive understanding of the internal dynamics, mass distribution, and intrinsic shape of elliptical galaxies. They help unravel the complex interplay between various physical processes shaping these galaxies and contribute to our understanding of their formation, evolution, and the role of dark matter in their dynamics.

3. Theoretical Models: Theoretical models play a crucial role in understanding the formation, evolution, and intrinsic shape of elliptical galaxies. These models incorporate physical processes and mechanisms to explain the observed properties of these galaxies. Here are some commonly used theoretical models for studying elliptical galaxies:

- **Monolithic Collapse:** The monolithic collapse model posits that elliptical galaxies form through a rapid and violent collapse of a gas-rich protogalactic cloud. In this scenario, the collapse leads to the formation of a spheroidal system without significant mergers. The collapse is assumed to be relatively quick, resulting in a predominantly old stellar population. This model can explain the smooth, featureless appearance of elliptical galaxies and their relatively uniform stellar populations.
- **Hierarchical Merging:** The hierarchical merging model suggests that elliptical galaxies form through a series of mergers and accretion events. According to this model, smaller galaxies merge over time, building up the mass and size of elliptical galaxies. These mergers lead to the reshaping of the galaxies, as well as the mixing of

stellar populations from the merging systems. Hierarchical merging can account for the observed diversity in shapes and stellar populations of elliptical galaxies.

- **Dynamical Modeling:** Dynamical modeling involves simulating the gravitational interactions and dynamics within elliptical galaxies. These models aim to understand the internal motions of stars and the distribution of mass within the galaxies. Various techniques, such as N-body simulations and dynamical modeling based on orbit libraries, are used to explore the range of possible orbits and shapes consistent with the observed kinematic data. Dynamical modeling helps determine the triaxiality (deviation from a perfect sphere or ellipsoid) of elliptical galaxies and the role of dark matter in shaping their dynamics.
- **Simulations and N-body Modeling:** Simulations and N-body modeling involve using numerical techniques to simulate the formation and evolution of galaxies, including ellipticals. These models incorporate the laws of physics, including gravity and gas dynamics, to follow the evolution of the system over time. Simulations can explore the effects of various physical processes, such as gas cooling, star formation, feedback from supernovae, and black hole activity, on the formation and shaping of elliptical galaxies.
- **Halo Occupation Distribution (HOD) Models:** Halo occupation distribution models relate the distribution of galaxies within dark matter halos. These models provide insights into how elliptical galaxies populate and distribute within the underlying dark matter halos. By combining observational constraints with theoretical predictions, HOD models can reproduce observed galaxy clustering statistics and provide information about the relationship between dark matter halos and elliptical galaxies.

These theoretical models are continually refined and updated based on observational data and advancements in computational techniques. They help us understand the physical processes driving the formation, evolution, and intrinsic shape of elliptical galaxies, as well as their connection to larger-scale structures in the universe.

4. Dynamical Modeling: Dynamical modeling is a powerful technique used to study the internal dynamics of elliptical galaxies and extract information about their mass distribution, intrinsic shape, and orbital structure. Here are some key aspects and approaches in dynamical modeling for elliptical galaxies:

- **Mass Modeling:** Dynamical models aim to determine the mass distribution within an elliptical galaxy. This involves constructing models that reproduce the observed kinematics, such as the velocity dispersion and rotation curves. Various techniques are used for mass modeling, including:
- **Jeans modeling:** This approach utilizes the Jeans equations, which relate the moments of the velocity distribution to the gravitational potential and mass density of the system. By solving these equations and comparing the model predictions with the observed kinematics, constraints on the mass distribution can be obtained.

- **Schwarzschild modeling:** Schwarzschild modeling is a more sophisticated approach that involves constructing dynamical models using orbit superposition techniques. It simulates the motions of a large number of individual stellar orbits and seeks the best-fitting model that reproduces the observed kinematics. Schwarzschild modeling can provide detailed information about the orbital structure and stellar populations within the galaxy.
- **Triaxial Models:** Triaxial models account for the fact that elliptical galaxies are not perfectly spheroidal but can have different axial ratios along different axes. Triaxial modeling aims to determine the intrinsic shape and orientation of the galaxy by comparing the predicted kinematics from models with the observed data. These models often involve assumptions about the mass distribution, such as triaxial ellipsoids or more complex shapes like prolate or oblate spheroids.
- **Dark Matter Modeling:** Dynamical modeling can also incorporate the effects of dark matter on the observed kinematics of elliptical galaxies. By assuming a dark matter halo profile, such as a Navarro-Frenk-White (NFW) profile, dynamical models can provide insights into the distribution and contribution of dark matter to the galaxy's mass distribution and dynamics. This allows researchers to study the interplay between dark matter and visible matter in shaping the galaxy's dynamics.
- **Anisotropy and Orbital Structure:** Dynamical models can also provide information about the anisotropy of stellar motions and the orbital structure within elliptical galaxies. By examining the observed velocity dispersion profiles and higher-order velocity moments, models can constrain the degree of radial or tangential anisotropy and provide insights into the orbital composition (e.g., radial, circular, or box orbits) within the galaxy.
- **Comparison with Observational Data:** The success of dynamical modeling relies on comparing the model predictions with observational data. This includes fitting the predicted kinematics to the observed velocity dispersion profiles, rotation curves, and higher-order velocity moments. The comparison is typically done using statistical techniques, such as maximum likelihood or Markov Chain Monte Carlo (MCMC) methods, to determine the best-fitting model parameters and quantify uncertainties.

Dynamical modeling is a complex process that requires detailed observational data and computational techniques to explore the vast parameter space of possible models. By combining dynamical modeling with other observational constraints, such as photometric data and stellar populations, researchers can obtain a comprehensive understanding of the internal dynamics, mass distribution, and intrinsic shape of elliptical galaxies.

5. **Simulations and N-body Modeling:** Simulations and N-body modeling are powerful tools used to study the formation, evolution, and intrinsic properties of elliptical galaxies. These computational techniques simulate the behavior of a large number of particles (representing stars, dark matter, and gas) under the influence of gravity and other physical processes. Here's an overview of simulations and N-body modeling for elliptical galaxies.

- **Cosmological Simulations:** Cosmological simulations aim to study the formation and evolution of galaxies within the framework of the evolving universe. These simulations start from the initial conditions of the early universe and follow the gravitational collapse and subsequent hierarchical merging of dark matter halos. By incorporating baryonic physics, such as gas cooling, star formation, and feedback processes, cosmological simulations can predict the formation and properties of elliptical galaxies within their cosmological context.
- **Galaxy Merger Simulations:** Galaxy merger simulations focus on the specific process of galaxy interactions and mergers that contribute to the formation of elliptical galaxies. These simulations typically start with two or more galaxies and simulate their gravitational interaction and merger. By varying the initial conditions (masses, orientations, gas fractions, etc.) and incorporating the physics of gas dynamics and star formation, merger simulations can explore the effects of mergers on the resulting morphology, kinematics, and stellar populations of elliptical galaxies.
- **N-body Simulations:** N-body simulations are numerical simulations that follow the gravitational interactions among a large number of particles representing stars, dark matter, and gas. These simulations can be used to study the internal dynamics and structure of elliptical galaxies. By modeling the gravitational forces and interactions, N-body simulations can reproduce the observed kinematics, density profiles, and other properties of elliptical galaxies. These simulations often incorporate additional physics, such as stellar evolution and feedback processes, to better match observations.
- **Stellar Population Synthesis:** Stellar population synthesis models are combined with simulations to study the properties of stars within elliptical galaxies. These models predict the spectral energy distributions and colors of stellar populations based on their age, metallicity, and other parameters. By combining simulated star formation histories with stellar population synthesis models, researchers can generate synthetic observations and compare them with real data to understand the stellar content and evolution of elliptical galaxies.
- **Hybrid Simulations:** Hybrid simulations combine N-body techniques with hydrodynamics to model the interplay between gas dynamics and stellar dynamics within galaxies. These simulations are particularly useful for studying the role of gas in the formation and shaping of elliptical galaxies. By including gas cooling, star formation, and feedback processes, hybrid simulations can reproduce the observed properties of elliptical galaxies, such as their gas content, metallicity gradients, and the connection between gas and star formation.

Simulations and N-body modeling allow researchers to explore a wide range of physical processes and parameters that shape elliptical galaxies. They provide a way to test theoretical models, reproduce observational data, and gain insights into the complex interplay between gravity, gas dynamics, star formation, and feedback mechanisms. By comparing the results of simulations with observations, scientists can refine our understanding of the formation, evolution, and intrinsic properties of elliptical galaxies.

VI. RESULTS AND KEY FINDINGS

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1. Triaxiality and Deviation from Perfect Ellipsoids: Triaxiality refers to the deviation of an object, such as an elliptical galaxy, from being a perfect ellipsoid or a sphere. It is a measure of the elongation and shape asymmetry along different axes. In the context of elliptical galaxies, triaxiality provides valuable information about their intrinsic shape and the presence of internal structure or asymmetry. Here's a closer look at triaxiality and the deviation from perfect ellipsoids:

- **Triaxial Ellipsoids:** A triaxial ellipsoid is an ellipsoid with different semi-axes lengths along its three orthogonal axes. In the case of elliptical galaxies, a triaxial ellipsoid implies that the galaxy's major, intermediate, and minor axes have different lengths. This results in a departure from a perfect sphere or a prolate/oblate ellipsoid.
- **Intrinsic Shape Parameters:** Triaxiality in elliptical galaxies can be quantified using intrinsic shape parameters. Some commonly used shape parameters include axial ratios and intrinsic ellipticities. Axial ratios compare the lengths of the major, intermediate, and minor axes, while intrinsic ellipticities measure the departure of the galaxy's shape from a perfect ellipse.
- **Observational Methods:** Determining the triaxiality of elliptical galaxies is challenging because it requires measuring the galaxy's intrinsic shape rather than its projected shape on the sky. However, several observational techniques can provide insights into the triaxial nature of ellipticals:
- **Kinematic Methods:** Observing the rotation, velocity dispersion, and higher-order velocity moments of stars within elliptical galaxies can reveal information about their intrinsic shape and the presence of triaxiality.
- **Surface Brightness and Isophote Analysis:** Studying the distribution of surface brightness and isophotes in elliptical galaxies can provide clues about their intrinsic shape. Departures from perfect ellipses, boxy or disk isophotes, and asymmetries indicate the presence of triaxiality.
- **X-ray and Radio Observations:** Observations in X-ray and radio wavelengths can trace the distribution of hot gas and radio-emitting structures within elliptical galaxies. The morphology and asymmetry of these components can provide evidence for triaxiality.
- **Importance of Triaxiality:** Triaxiality is essential because it reflects the complex formation and evolutionary processes that shape elliptical galaxies. Triaxial galaxies can result from major mergers, accretion events, or dynamical instabilities. The

presence of triaxiality influences the distribution of mass, the orbits of stars, and the overall dynamics of the galaxy. Understanding the triaxial nature of elliptical galaxies helps constrain their formation mechanisms and the role of various physical processes involved.

- **Modeling Triaxial Galaxies:** Theoretical models, such as dynamical models and numerical simulations, can be used to generate triaxial galaxy models. These models aim to reproduce the observed kinematics and morphology of triaxial galaxies, providing insights into their formation scenarios, orbital structures, and mass distributions. Comparing the predictions of these models with observational data can help constrain the triaxiality and internal structures of elliptical galaxies.

By investigating the triaxiality and deviation from perfect ellipsoids, scientists gain a deeper understanding of the complexities in the formation, dynamics, and evolutionary history of elliptical galaxies. Triaxiality is an important parameter to consider when studying the intrinsic shape and structural properties of these fascinating astronomical objects.

2. Connection Between Shape and Stellar Population: The shape of an elliptical galaxy and its stellar populations are interconnected and provide valuable insights into the formation and evolutionary history of these galaxies. Here are some key connections between the shape of elliptical galaxies and their stellar populations:

- **Formation Mechanisms:** The shape of an elliptical galaxy can provide clues about the dominant formation mechanism involved. For example, a spherical or oblate shape is often associated with monolithic collapse or dissipative mergers, where gas-rich material settles into a rotationally supported disk before the collapse. On the other hand, a more triaxial shape may indicate a formation process involving multiple mergers and interactions between galaxies.
- **Age and Metallicity Gradients:** The stellar populations within an elliptical galaxy can exhibit gradients in age and metallicity, with the central regions often hosting older and more metal-rich stars. These gradients can be related to the galaxy's shape. Studies have found that more flattened and elongated ellipticals tend to have stronger gradients in stellar age and metallicity, suggesting a history of dissipative processes like gas inflows or merger events that led to the formation of a central concentration of older, metal-rich stars.
- **Color-Magnitude Relations:** The shape of an elliptical galaxy is also linked to its position in color-magnitude relations. These relations show a correlation between the galaxy's luminosity (magnitude) and its color, which is often used as an indicator of stellar populations. Ellipticals that are more spheroidal or rounder tend to exhibit redder colors, indicating a dominance of older stellar populations. In contrast, flatter and more elongated ellipticals may have bluer colors, suggesting the presence of younger stars or ongoing star formation.

- **Orbital Structures:** The shape of an elliptical galaxy is closely tied to its orbital structure, which, in turn, affects the stellar populations within the galaxy. Triaxial or more flattened ellipticals tend to have more complex and diverse orbital structures. These structures can lead to a mixing of stellar populations and a more homogeneous distribution of stars throughout the galaxy. Flatter ellipticals may also exhibit a larger fraction of box or tube orbits, while more spherical galaxies may have predominantly radial or isotropic orbits.
- **Merger History:** The shape of an elliptical galaxy can provide insights into its merger history and subsequent impact on stellar populations. Major mergers involving galaxies of similar mass tend to produce more spherical or oblate ellipticals, whereas minor mergers or interactions can lead to more triaxial shapes. The mergers can trigger star formation, resulting in a mix of young and old stellar populations. The specific shape and alignment of tidal features, such as shells or streams, can also provide information about the direction and orientation of past merger events.

Understanding the connection between the shape and stellar populations of elliptical galaxies helps unravel their formation mechanisms, the interplay between different evolutionary processes, and the role of mergers in shaping their structure and stellar content. By studying these connections, astronomers gain valuable insights into the complex processes that govern the evolution of elliptical galaxies.

3. Role of Mergers and Environmental Effects: Mergers and environmental effects play significant roles in shaping the properties and evolution of elliptical galaxies. Here's an overview of their impact:

- **Mergers:** Mergers occur when two or more galaxies come together and gravitationally interact. They are thought to be a key driver of the formation and evolution of elliptical galaxies. The effects of mergers on ellipticals include:
- **Galaxy Transformation:** Major mergers involving gas-rich galaxies can trigger intense star formation and lead to the formation of ellipticals. The gravitational interaction causes gas inflows, shocks, and compressions, leading to the formation of new stars. The resulting elliptical galaxy may inherit some of the properties, such as kinematics and stellar populations, from its progenitor galaxies.
- **Size and Mass Growth:** Mergers can significantly increase the size and mass of elliptical galaxies. The combination of stellar mass from the merging galaxies contributes to the growth of the final elliptical. Additionally, the redistribution of mass during mergers can result in structural changes and the formation of a more centrally concentrated system.
- **Morphological Transformation:** Mergers can cause a transformation in the morphology of galaxies, leading to the formation of ellipticals. Disk galaxies that undergo mergers can lose their organized disk structure, resulting in a more spheroidal or elliptical appearance.

- **Environmental Effects:** The environment in which an elliptical galaxy resides can also influence its properties and evolution. Key environmental effects include:
- **Galaxy Interactions:** Interactions between galaxies within a dense environment, such as galaxy clusters, can induce tidal forces, triggering mergers or tidal interactions. These interactions can disrupt the morphology, kinematics, and stellar populations of elliptical galaxies.
- **Galaxy Stripping and Cannibalism:** In galaxy clusters, gravitational interactions can lead to the stripping of stars and gas from smaller satellite galaxies. Larger ellipticals in the cluster can grow by accreting and merging with the stripped material, leading to the buildup of their stellar mass.
- **Galaxy Merging Hierarchy:** The hierarchical growth of galaxy clusters can influence the properties of elliptical galaxies. Smaller groups or galaxies merge to form larger galaxy clusters, which can subsequently merge to form even more massive clusters. This merging hierarchy affects the formation and evolution of elliptical galaxies within these clusters.

Both mergers and environmental effects contribute to the diversity of properties observed among elliptical galaxies. They influence the structural characteristics, stellar populations, gas content, and kinematics of these galaxies. Studying the impact of mergers and environmental effects helps us understand the formation mechanisms, evolutionary pathways, and the role of external factors in shaping the properties of elliptical galaxies.

- 4. Implications for Galaxy Evolution:** The role of mergers and environmental effects in shaping the properties of elliptical galaxies has important implications for galaxy evolution. Here are some key implications:
- **Galaxy Formation and Assembly:** Mergers and interactions play a significant role in the formation and assembly of elliptical galaxies. Major mergers of gas-rich galaxies can trigger intense starbursts and lead to the formation of massive, centrally concentrated ellipticals. The hierarchical growth of galaxy clusters through mergers and accretion of smaller systems also contributes to the assembly of ellipticals within these dense environments.
 - **Morphological Transformation:** Mergers and environmental effects can drive the morphological transformation of galaxies from disk-dominated systems to spheroidal or elliptical structures. Interactions and mergers disrupt the organized disk structure, while environmental processes like ram pressure stripping and harassment can further alter the morphology. Understanding these transformations is crucial for unraveling the connection between the early universe's gas-rich galaxies and the formation of elliptical galaxies.
 - **Stellar Population Evolution:** Mergers and interactions can induce star formation through gas inflows and shocks, resulting in a mix of stellar populations in elliptical galaxies. The merging of galaxies with different stellar populations can create

composite systems with a range of ages and metallicities. Additionally, environmental effects such as ram pressure stripping and galaxy cannibalism can deplete the gas reservoir and stifle ongoing star formation, leading to the formation of predominantly old and metal-rich stellar populations in ellipticals.

- **Size and Mass Growth:** Mergers contribute to the size and mass growth of elliptical galaxies. Major mergers can lead to a significant increase in the stellar mass by combining the progenitor galaxies' stellar content. The redistribution of mass during mergers can also result in the formation of more centrally concentrated systems. The hierarchical growth of galaxy clusters through mergers and accretion can further contribute to the growth of ellipticals within these dense environments.
- **Environmental Influence:** The environment in which elliptical galaxies reside influences their properties and evolution. Dense environments, such as galaxy clusters, can subject ellipticals to various environmental effects like ram pressure stripping, harassment, and cannibalism. These processes can modify the gas content, star formation activity, and structural properties of elliptical galaxies. The environmental influence helps shape the observed population of ellipticals and contributes to the formation of red sequence galaxies in galaxy clusters.

Understanding the implications of mergers and environmental effects for galaxy evolution provides insights into the mechanisms driving the formation, transformation, and growth of elliptical galaxies. These processes help shape the observed properties, stellar populations, and structural characteristics of ellipticals, providing important constraints for theoretical models and our understanding of the broader context of galaxy evolution.

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